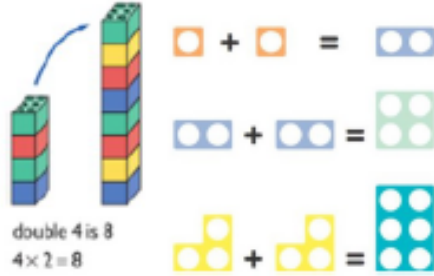

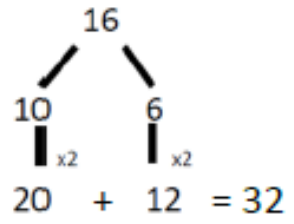
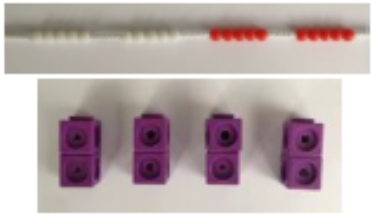
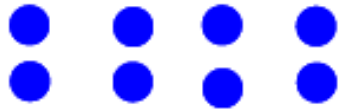
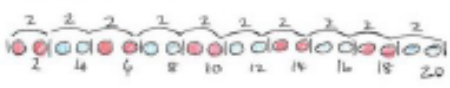
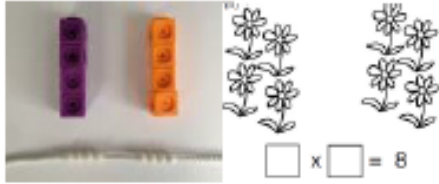

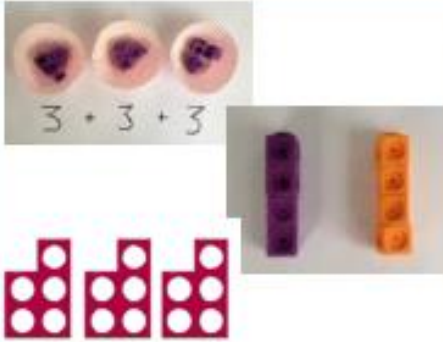
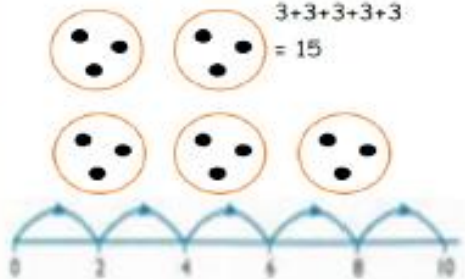

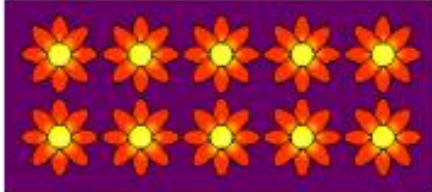
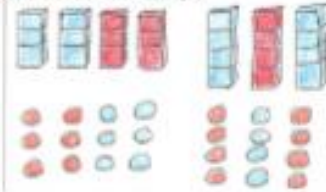
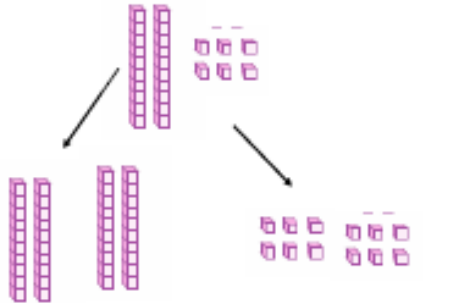
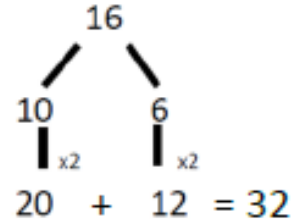
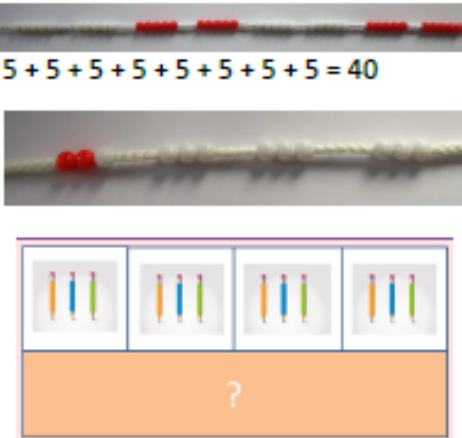
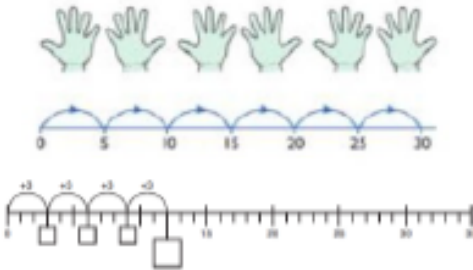
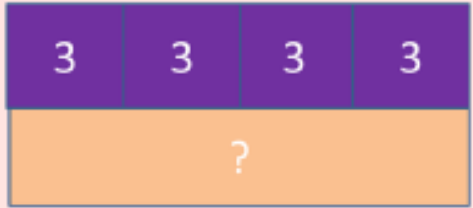


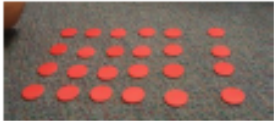




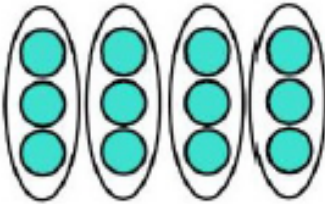
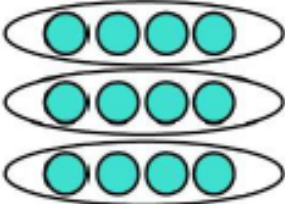



Objective & Strategy	Concrete	Pictorial	Abstract
<p><b>Doubling</b></p>	<p>Use practical activities using manipulatives including cubes and Numicon to demonstrate doubling</p>  <p>double 4 is 8 <math>4 \times 2 = 8</math></p>	<p>Draw pictures to show how to double numbers</p> <p>Double 4 is 8</p> 	<p>Partition a number and then double each part before recombining it back together.</p> 
<p><b>Counting in multiples</b></p>	<p>Count the groups as children are skip counting, children may use their fingers as they are skip counting.</p> 	 <p>Children make representations to show counting in multiples.</p> 	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p>
<p><b>Making equal groups and counting the total</b></p>	 <p>Use manipulatives to create equal groups.</p> <p><math>\square \times \square = 8</math></p>	<p>Draw  to show <math>2 \times 3 = 6</math></p> <p>Draw and make representations</p>	<p><math>2 \times 4 = 8</math></p>

Objective & Strategy	Concrete	Pictorial	Abstract
Repeated addition	 <p>Use different objects to add equal groups</p>	<p>Use pictorial including number lines to solve prob</p> <p>There are 3 sweets in one bag. How many sweets are in 5 bags altogether?</p> 	<p>Write addition sentences to describe objects and pictures.</p> 
Understanding arrays	<p>Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.</p> 	<p>Draw representations of arrays to show understanding</p> 	$3 \times 2 = 6$ $2 \times 5 = 10$

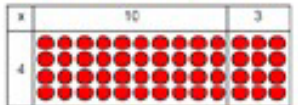
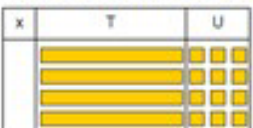

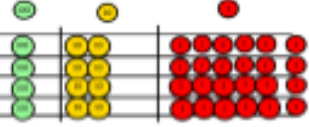

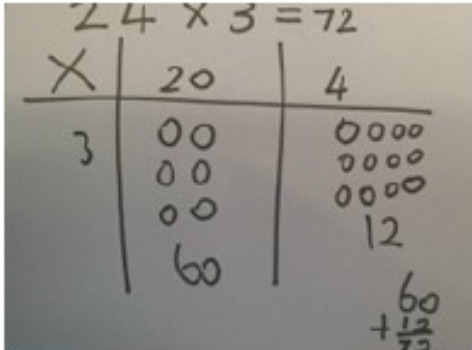
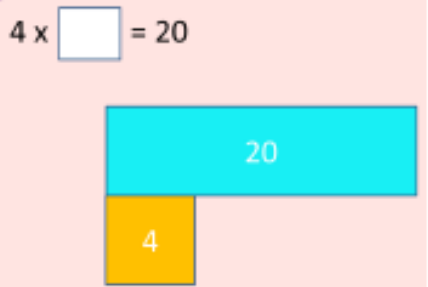
# Y1

# MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract
<p>Doubling</p>	<p>Model doubling using dienes and PV counters.</p>  <p><math>40 + 12 = 52</math></p>	<p>Draw pictures and representations to show how to double numbers</p>	<p>Partition a number and then double each part before recombining it back together.</p>  <p><math>20 + 12 = 32</math></p>
<p>Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)</p>	<p>Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar models.</p>  <p><math>5 + 5 + 5 + 5 + 5 + 5 + 5 = 40</math></p> <p>?</p>	<p>Number lines, counting sticks and bar models should be used to show representation of counting in multiples.</p>   <p>?</p>	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>0, 2, 4, 6, 8, 10</p> <p>0, 3, 6, 9, 12, 15</p> <p>0, 5, 10, 15, 20, 25, 30</p> <p><math>4 \times 3 = \square</math></p>



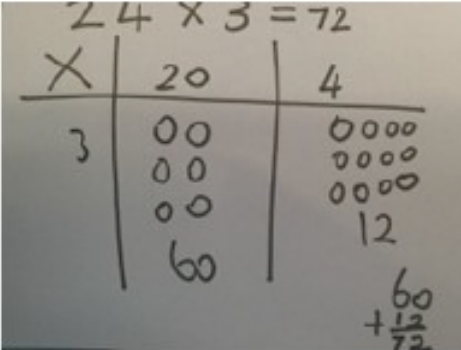
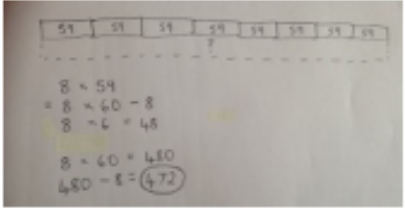
Objective & Strategy	Concrete	Pictorial	Abstract
<p>Multiplication is commutative</p>	<p>Create arrays using counters and cubes and Numicon.</p>    <p>Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.</p>  	<p>Use representations of arrays to show different calculations and explore commutativity.</p>  	<p><math>12 = 3 \times 4</math></p> <p><math>12 = 4 \times 3</math></p> <div style="border: 1px solid black; padding: 5px;"> <p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p><math>5 + 5 + 5 = 15</math></p> <p><math>3 + 3 + 3 + 3 + 3 = 15</math></p> <p><math>5 \times 3 = 15</math></p> <p><math>3 \times 5 = 15</math></p> </div>
<p>Using the Inverse</p> <p><i>This should be taught alongside division, so pupils learn how they work alongside each other.</i></p>		 <p> <input type="checkbox"/> <math>\times</math> <input type="checkbox"/> = <input type="checkbox"/>  <input type="checkbox"/> <math>\times</math> <input type="checkbox"/> = <input type="checkbox"/>  <input type="checkbox"/> <math>\div</math> <input type="checkbox"/> = <input type="checkbox"/>  <input type="checkbox"/> <math>\div</math> <input type="checkbox"/> = <input type="checkbox"/> </p>	<p><math>2 \times 4 = 8</math></p> <p><math>4 \times 2 = 8</math></p> <p><math>8 \div 2 = 4</math></p> <p><math>8 \div 4 = 2</math></p> <p><math>8 = 2 \times 4</math></p> <p><math>8 = 4 \times 2</math></p> <p><math>2 = 8 \div 4</math></p> <p><math>4 = 8 \div 2</math></p> <p>Show all 8 related fact family sentences.</p>




# Y3 MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract															
<p><b>Grid method</b></p>	<p>Show the links with arrays to first introduce the grid method</p>  <p>4 rows of 10 4 rows of 3</p> <p>Move onto base ten to move towards a more compact method.</p>  <p>4 rows of 13</p> <p>Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows</p>  <p>Calculations <math>4 \times 126</math></p> <p>Fill each row with 126</p>  <p>Calculations <math>4 \times 126</math></p> <p>Add up each column, starting with the ones making any exchanges needed</p>  <p>Then you have your answer.</p>	<p>Children can represent their work with place value counters in a way that they understand.</p> <p>They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.</p>  <p>Bar model are used to explore missing numbers</p> 	<p>Start with multiplying by one digit numbers and showing the clear addition alongside the grid.</p> <table border="1" data-bbox="1444 502 1758 590"> <tr> <td>x</td> <td>30</td> <td>5</td> </tr> <tr> <td>7</td> <td>210</td> <td>35</td> </tr> </table> <p><math>210 + 35 = 245</math></p> <p>Moving forward, multiply by a 2 digit number showing the different rows within the grid method.</p> <table border="1" data-bbox="1467 869 1747 1061"> <tr> <td></td> <td>10</td> <td>8</td> </tr> <tr> <td>10</td> <td>100</td> <td>80</td> </tr> <tr> <td>3</td> <td>30</td> <td>24</td> </tr> </table>	x	30	5	7	210	35		10	8	10	100	80	3	30	24
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# Y4 MULTIPLICATION X

Objective & Strategy	Concrete	Pictorial	Abstract																																																			
<p>Grid method recap from year 3 for 2 digits x 1 digit</p> <p>Move to multiplying 3 digit numbers by 1 digit. (year 4 expectation)</p>	<p>Use place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows</p>  <p>Calculations <math>4 \times 126</math></p> <p>Fill each row with 126</p>  <p>Add up each col making any exchanges needed</p>	<p>Children can represent their work with place value counters in a way that they understand.</p> <p>They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.</p> 	<p>Start with multiplying by one digit numbers and showing the clear addition alongside the grid.</p> <table border="1" data-bbox="1429 497 1731 587"> <tr> <td>x</td> <td>30</td> <td>5</td> </tr> <tr> <td>7</td> <td>210</td> <td>35</td> </tr> </table> <p><math>210 + 35 = 245</math></p>	x	30	5	7	210	35																																													
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<p>Column multiplication</p>	<p>Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. <math>321 \times 2 = 642</math></p> <table border="1" data-bbox="371 1093 683 1460"> <thead> <tr> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> </tr> </tbody> </table> <p>It is important at this stage that they always multiply the ones first.</p> <p>The corresponding long multiplication is modelled alongside</p>	Hundreds	Tens	Ones													<p>The grid method may be used to show how this relates to a formal written method.</p>  <p>Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.</p>	<table border="1" data-bbox="936 981 1258 1061"> <tr> <td>x</td> <td>300</td> <td>20</td> <td>7</td> </tr> <tr> <td>4</td> <td>1200</td> <td>80</td> <td>28</td> </tr> </table> <p style="text-align: center;">→</p> <table border="1" data-bbox="1489 965 1668 1316"> <tr> <td></td> <td>327</td> </tr> <tr> <td>x</td> <td>4</td> </tr> <tr> <td colspan="2"><hr/></td> </tr> <tr> <td></td> <td>28</td> </tr> <tr> <td></td> <td>80</td> </tr> <tr> <td></td> <td>1200</td> </tr> <tr> <td></td> <td><hr/></td> </tr> <tr> <td></td> <td>1308</td> </tr> </table> <p style="text-align: center;">↻</p> <table border="1" data-bbox="1377 1348 1601 1508"> <tr> <td></td> <td>327</td> </tr> <tr> <td>x</td> <td>4</td> </tr> <tr> <td colspan="2"><hr/></td> </tr> <tr> <td></td> <td>1308</td> </tr> <tr> <td></td> <td><hr/></td> </tr> <tr> <td></td> <td>1308</td> </tr> </table> <p>This may lead to a compact method.</p>	x	300	20	7	4	1200	80	28		327	x	4	<hr/>			28		80		1200		<hr/>		1308		327	x	4	<hr/>			1308		<hr/>		1308
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Objective & Strategy	Concrete	Pictorial	Abstract																																					
<p>Column Multiplication for 3 and 4 digits x 1 digit.</p>	<table border="1" data-bbox="387 363 712 746"> <thead> <tr> <th>Hundreds</th> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> </tr> </tbody> </table> <p>It is important at this stage that they always multiply the ones first.</p> <p>Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. <math>321 \times 2 = 642</math></p>	Hundreds	Tens	Ones													<table border="1" data-bbox="965 379 1294 459"> <tr> <td>x</td> <td>300</td> <td>20</td> <td>7</td> </tr> <tr> <td>4</td> <td>1200</td> <td>80</td> <td>28</td> </tr> </table> 	x	300	20	7	4	1200	80	28	<table data-bbox="1518 379 1697 746"> <tr> <td>327</td> </tr> <tr> <td>x 4</td> </tr> <tr> <td>-----</td> </tr> <tr> <td>28</td> </tr> <tr> <td>80</td> </tr> <tr> <td>1200</td> </tr> <tr> <td>-----</td> </tr> <tr> <td>1308</td> </tr> </table>  <table border="1" data-bbox="1406 767 1630 943"> <tr> <td>327</td> </tr> <tr> <td>x 4</td> </tr> <tr> <td>-----</td> </tr> <tr> <td>1308</td> </tr> <tr> <td>1 2</td> </tr> </table> <p>This will lead to a compact method.</p>	327	x 4	-----	28	80	1200	-----	1308	327	x 4	-----	1308	1 2	
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<p>Column multiplication</p>	<p>Manipulatives may still be used with the corresponding long multiplication modelled alongside.</p>	<table border="1" data-bbox="902 1018 1205 1225"> <tr> <td></td> <td>10</td> <td>8</td> </tr> <tr> <td>10</td> <td>100</td> <td>80</td> </tr> <tr> <td>3</td> <td>30</td> <td>24</td> </tr> </table>  <p>Continue to use bar modelling to support problem solving</p>		10	8	10	100	80	3	30	24	<table border="1" data-bbox="1395 1002 1630 1257"> <tr> <td></td> <td>18</td> </tr> <tr> <td>x 13</td> <td></td> </tr> <tr> <td>-----</td> <td></td> </tr> <tr> <td>54</td> <td></td> </tr> <tr> <td>2</td> <td></td> </tr> <tr> <td>180</td> <td></td> </tr> <tr> <td>-----</td> <td></td> </tr> <tr> <td>234</td> </tr> </table> <p>18 x 3 on the first row (8 x 3 = 24, carrying the 2 for 20, then 1 x 3) 18 x 10 on the 2nd row. Show multiplying by 10 by putting zero in units first</p> <table border="1" data-bbox="1406 1321 1697 1528"> <tr> <td>1234</td> <td></td> </tr> <tr> <td>x 6</td> <td></td> </tr> <tr> <td>-----</td> <td></td> </tr> <tr> <td>7404</td> <td>(1234 x 6)</td> </tr> <tr> <td>12340</td> <td>(1234 x 10)</td> </tr> <tr> <td>-----</td> <td></td> </tr> <tr> <td>19744</td> </tr> </table>		18	x 13		-----		54		2		180		-----		234	1234		x 6		-----		7404	(1234 x 6)	12340	(1234 x 10)	-----		19744
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Objective & Strategy	Concrete	Pictorial	Abstract
Multiplying decimals up to 2 decimal places by a single digit.			<p>Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer.</p> $\begin{array}{r} 3.19 \\ \times 8 \\ \hline 25.52 \end{array}$

**Y6**  
**MULTIPLICATION X**